## Mutually-Recursive Data Definitions

## CS 5010 Program Design Paradigms "Bootcamp"

 Lesson 6.4
## Mutually Recursive Data Definitions

- Sometimes two kinds of data are intertwined
- In this lesson, we'll consider an easy example: alternating lists
- An alternating list is a list whose elements alternate between numbers and strings


## Learning Objectives

- At the end of this lesson, the student should be able to
- recognize information that should be represented as an alternating list
- write a data definition for an alternating list
- explain why templates for alternating lists come in pairs


## Alternating Lists

- Let's write a data definition for lists whose elements alternate between numbers and strings.


## Data Definitions

; ; A ListOfAlternatingNumbersAndStrings
(LANS) is one of:
; ; -- empty
; ; -- (cons Number LASN)
; ; A ListOfAlternatingStringsAndNumbers (LASN) is one of:
; ; -- empty
; ; -- (cons String LANS)

A LANS is a list of alternating numbers and strings, starting with a number. A LASN is a list of alternating numbers and strings, starting with a string. Either can be empty. Note that the rest of a non-empty LANS is a LASN, and vice-versa.

## Examples



## These data definitions are mutually recursive

; ; A ListOfAlternatingNumbersAndStrings
(LANS) is one of:
; ; -- empty
; ; -- (cons Number LASN)
; ; A ListOfAlternatingStringsAndNumbers
(LASN) is one
; ; -- empty
; ; -- (cons String LANS)

The definition of a LANS depends on LASN, and the definition of a LASN depends on LANS.

## This is mutual recursion



LASN LANS

defined in terms of

## The template recipe

| Question | Answer |
| :--- | :--- |
| Does the data definition distinguish <br> among different subclasses of data? | Your template needs as many cond <br> clauses as subclasses that the data <br> definition distinguishes. |
| How do the subclasses differ from each <br> other? | Use the differences to formulate a <br> condition per clause. |
| Do any of the clauses deal with structured <br> values? | If so, add appropriate selector expressions <br> to the clause. |
| Does the data definition use self- <br> references? | Formulate "natural recursions" for the <br> template e to represent the self-references <br> of the data definition. |
| Do any of the fields contain compound or or <br> mixed data? | If the value of a field is a foo, add a call to <br> a foo-fn to use it. |

The template recipe doesn't need to change

## Templates come in pairs

; ; lans-fn : LANS -> ??
;; (define (lans-fn lans)
(cond
; [ [empty? lans) ...]

Here are the templates for LANS and LASN. Observe the recursive calls, in red.
; [else (...
(first lans)
(lasn-fn (rest lans)))]))
;; lasn-fn : LASN -> ??
;; (define (lasn-fn lasn)
;; (cond
; [ (empty? lasn) ...]
; $\quad$ [else (...
(first lasn)
(lans-fn (rest lasn)))]))

## Templates are mutually recursive

; ; lans-fn : LANS -> ??
; ; (define (lans-fn lans)


## This is mutual recursion


lasn-fn

## lans-fn



Here's that same picture, this time describing the recursive calls in the template.

## The template questions



What is the answer for the empty LANS?

If you knew the answer for the LASN inside the LANS, what would the answer be for the whole LANS?

## One function, one task

- Each function deals with exactly one data definition.
- So functions will come in pairs
- Write contracts and purpose statements together, or
- Write one, and the other one will appear as a wishlist function


## Example

lans-sum : LANS -> Number
Returns the sum of all the numbers in the given Lans
lasn-sum : LASN -> Number
Returns the sum of all the numbers in the given Lasn

Here's an example of a pair of functions that should go together.

## Examples

(lans-sum
(cons 23
(cons "foo"
(cons 11 empty)))) = 34
(lasn-sum
(cons "bar"
(cons 23
(cons "foo"
(cons 11 empty))))) = 34

## Strategy and Function Definitions

; ; strategy: Use template for LANS and LASN
;; lans-sum : LANS -> Number
(define (lans-sum lans)
(cond
[(empty? lans) 0]
[else (+
(first lans)
(lasn-sum (rest lans)))]))
; ; lasn-sum : LASN -> Number
(define (lasn-sum lasn)
(cond
[(empty? lasn) 0]
[else (lans-sum (rest lasn))]))

We apply the template by filling in each of the four blanks
with the answer to the corresponding template question.

## What are alternating lists good for?



## Alternating Lists

Answer: Not much! Don't use them!

But they make a good example of mutuallyrecursive data definitions

## Summary

- You should now be able to:
- recognize information that should be represented as an alternating list
- write a data definition for an alternating list
- explain why templates for alternating lists come in pairs


## Next Steps

- Study the file 06-4-lasns.rkt
- If you have questions about this lesson, ask them on the Discussion Board
- Do Guided Practice 6.4
- Go on to the next lesson

