Mutually-Recursive Data Definitions

CS 5010 Program Design Paradigms "Bootcamp" Lesson 6.4



Mutually Recursive Data Definitions

- Sometimes two kinds of data are intertwined
- In this lesson, we'll consider an easy example: alternating lists
- An alternating list is a list whose elements alternate between numbers and strings

Learning Objectives

- At the end of this lesson, the student should be able to
 - recognize information that should be represented as an alternating list
 - write a data definition for an alternating list
 - explain why templates for alternating lists come in pairs

Alternating Lists

 Let's write a data definition for lists whose elements alternate between numbers and strings.

Data Definitions

- ;; A ListOfAlternatingNumbersAndStrings
 (LANS) is one of:
- ;; -- empty
- ;; -- (cons Number LASN)
- ;; A ListOfAlternatingStringsAndNumbers
 (LASN) is one of:
- ;; -- empty
- ;; -- (cons String LANS)

A LANS is a list of alternating numbers and strings, starting with a number. A LASN is a list of alternating numbers and strings, starting with a string. Either can be empty. Note that the rest of a non-empty LANS is a LASN, and vice-versa.

Examples

- empty is a LASN
- (cons 11 empty) is a LANS
- (cons "foo" (cons 11 empty)) is a LASN
- (cons 23 (cons "foo" (cons 11 empty))) is a LANS
- (cons "bar" (cons 23 (cons "foo" (cons 11 empty)))) is a LASN

These data definitions are *mutually recursive*

- ;; A ListOfAlternatingNumbersAndStrings
 (LANS)_is one of:
- ;; -- empty
- ;; -- (cons Number LASN)
- ;; A ListOfAlternatingStringsAndNumbers
 (LASN) is one of;
- ;; -- empty
- ;; -- (cons String LANS)

The definition of a LANS depends on LASN, and the definition of a LASN depends on LANS.



The template recipe

Question	Answer
Does the data definition distinguish among different subclasses of data?	Your template needs as many <u>cond</u> clauses as subclasses that the data definition distinguishes.
How do the subclasses differ from each other?	Use the differences to formulate a condition per clause.
Do any of the clauses deal with structured values?	If so, add appropriate selector expressions to the clause.
Does the data definition use self- references?	Formulate ``natural recursions" for the template to represent the self-references of the data definition.
Do any of the fields contain compound or mixed data?	If the value of a field is a foo, add a call to a foo-fn to use it.

The template recipe doesn't need to change

Templates come in pairs

```
lans-fn : LANS -> ??
::
   (define (lans-fn lans)
;;
     (cond
;;
       [(empty? lans) ...]
;;
       [else (...
;;
;;
                (first lans)
                (lasn-fn (rest lans)))]))
;;
   lasn-fn : LASN -> ??
   (define (lasn-fn lasn)
     (cond
;;
;;
       [(empty? lasn) ...]
       [else (...
;;
                (first lasn)
;;
                (lans-fn (rest lasn)))]))
;;
```

Here are the templates for LANS and LASN. Observe the recursive calls, in red.

Templates are mutually recursive

```
lans-fn : LANS -> ??
   (define (lans-fn lans)
;;
     (cond
;;
       [(empty?] lans) ...]
;;
       [else (.
;;
;;
                 (first lans)
                 [lasn-fn (rest lans)))]))
;;
   ;; lasn-fn <∕ ∠A$N -> ??
   (define (lasn-fn lasn)
     (cond
;;
       [(empty? lash) ...]
;;
       [else (...
;;
                (first lasn)
;;
                (lans-fn (rest lasn)))]))
;;
```





One function, one task

- Each function deals with exactly one data definition.
- So functions will come in pairs
- Write contracts and purpose statements together, or
- Write one, and the other one will appear as a wishlist function

Example

lans-sum : LANS -> Number Returns the sum of all the numbers in the given Lans

lasn-sum : LASN -> Number
Returns the sum of all the numbers
in the given Lasn

Here's an example of a pair of functions that should go together.

Examples

```
(lans-sum
 (cons 23
  (cons "foo"
   (cons 11 empty))))
                        = 34
(lasn-sum
  (cons "bar"
   (cons 23
    (cons "foo"
```

(cons 11 empty))))) = 34

And here are some examples for our two functions. Observe that **lans-sum** is applied to a **LANS**, and **lasn-sum** is applied to a **LASN**.

Strategy and Function Definitions

```
;; strategy: Use template for LANS and LASN
;; lans-sum : LANS -> Number
(define (lans-sum lans)
  (cond
    [(empty? lans) 0]
    [else (+
            (first lans)
            (lasn-sum (rest lans)))]))
;; lasn-sum : LASN -> Number
(define (lasn-sum lasn)
  (cond
    [(empty? lasn) 0]
    [else (lans-sum (rest lasn))]))
```

We apply the template by filling in each of the four blanks with the answer to the corresponding template question.



Answer: Not much! Don't use them!

But they make a good example of mutuallyrecursive data definitions

Summary

- You should now be able to:
 - recognize information that should be represented as an alternating list
 - write a data definition for an alternating list
 - explain why templates for alternating lists come in pairs

Next Steps

- Study the file 06-4-lasns.rkt
- If you have questions about this lesson, ask them on the Discussion Board
- Do Guided Practice 6.4
- Go on to the next lesson